

Next-generation radio interferometric imaging with compressive sensing

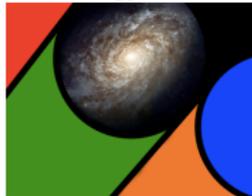
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University College London (UCL)*

Cosmology @ MSSL



Auckland University of Technology (AUT) :: December 2013

Outline

- 1 Radio Interferometry (RI)
- 2 Compressive Sensing (CS)
- 3 Radio Interferometric Imaging with Compressive Sensing (RI+CS)
- 4 Spread Spectrum
- 5 Continuous Visibilities
- 6 Outlook



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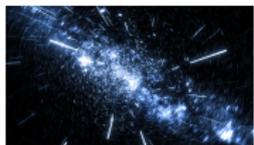


Next-generation of radio interferometry rapidly approaching

- **Square Kilometre Array (SKA)** first observations planned for 2019.
- Many other pathfinder telescopes under construction, *e.g.* LOFAR, ASKAP, MeerKAT, MWA.
- **New modelling and imaging techniques** required to ensure the next-generation of interferometric telescopes reach their full potential.



Figure: Artist impression of SKA dishes. [Credit: SKA Organisation]



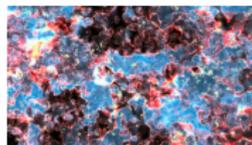
(a) Dark-energy



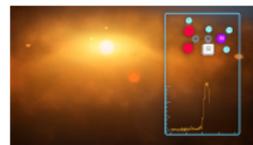
(b) GR



(c) Cosmic magnetism



(d) Epoch of reionization



(e) Exoplanets

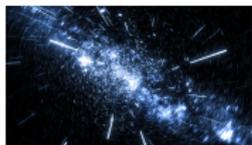
Figure: SKA science goals. [Credit: SKA Organisation]

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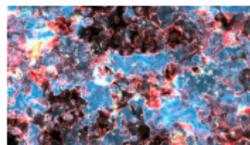
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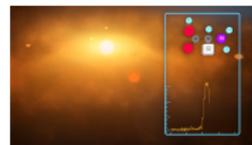
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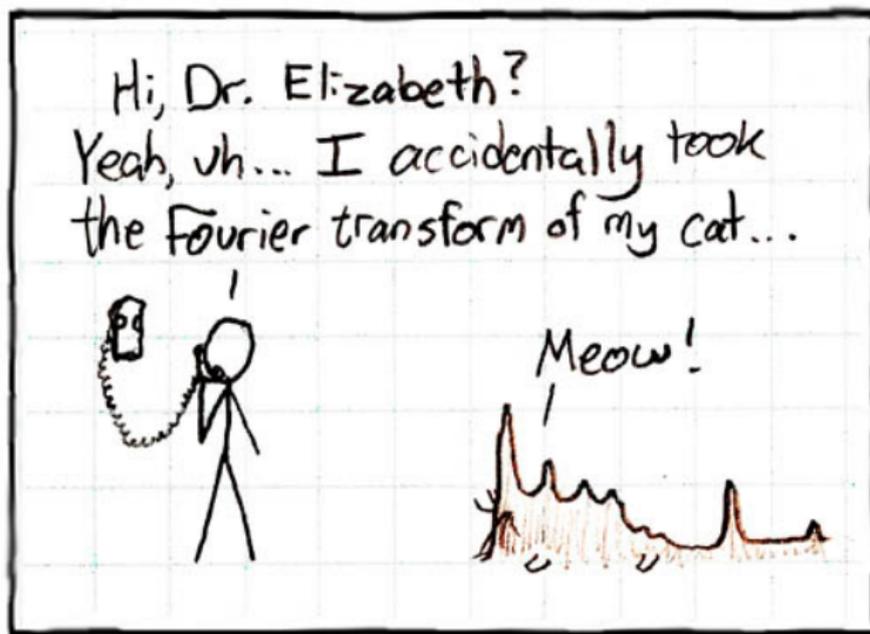
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Figure: SKA science goals. [Credit: SKA Organisation]

Fourier imaging



[Credit: xkcd]



Radio interferometry

- The **complex visibility** measured by an interferometer is given by

$$y(\mathbf{u}, w) = \int_{D^2} A(\mathbf{l}) x(\mathbf{l}) C(\|\mathbf{l}\|_2) e^{-i2\pi\mathbf{u}\cdot\mathbf{l}} \frac{d^2\mathbf{l}}{n(\mathbf{l})},$$

visibilities

where the **w-modulation** $C(\|\mathbf{l}\|_2)$ is given by

$$C(\|\mathbf{l}\|_2) \equiv e^{i2\pi w(1-\sqrt{1-\|\mathbf{l}\|^2})}.$$

w-modulation

- Various assumptions are often made regarding the size of the **field-of-view (FoV)**:

- Small-field with $\|\mathbf{l}\|^2 w \ll 1 \Rightarrow C(\|\mathbf{l}\|_2) \approx 1$

- Small-field with $\|\mathbf{l}\|^2 w \ll 1 \Rightarrow C(\|\mathbf{l}\|_2) \approx e^{i2\pi w \|\mathbf{l}\|^2}$

- Wide-field $\Rightarrow C(\|\mathbf{l}\|_2) = e^{i2\pi w(1-\sqrt{1-\|\mathbf{l}\|^2})}$



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- Small-field with $\|\mathbf{l}\|^2 w \ll 1$

\Rightarrow

$$C(\|\mathbf{l}\|_2) \simeq 1$$

- Small-field with $\|\mathbf{l}\|^4 w \ll 1$

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Radio interferometric inverse problem

- Consider the ill-posed inverse problem of radio interferometric imaging:

$$y = \Phi x + n,$$

where y are the measured visibilities, Φ is the linear measurement operator, x is the underlying image and n is instrumental noise.

- Measurement operator $\Phi = MFCA$ may incorporate:
 - primary beam A of the telescope;
 - w -modulation modulation C ;
 - Fourier transform F ;
 - masking M which encodes the incomplete measurements taken by the interferometer.



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Interferometric imaging: **recover an image from noisy and incomplete Fourier measurements.**



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Compressive sensing

“Nothing short of revolutionary.”

– National Science Foundation

- Developed by [Emmanuel Candes](#) and [David Donoho](#) (and others).



(a) Emmanuel Candes



(b) David Donoho



Compressive sensing

- Next evolution of wavelet analysis → wavelets are a key ingredient.
- The mystery of JPEG compression (discrete cosine transform; wavelet transform).
- Move compression to the acquisition stage → [compressive sensing](#).
- [Acquisition](#) versus [imaging](#).



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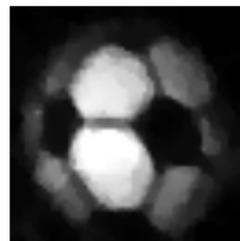
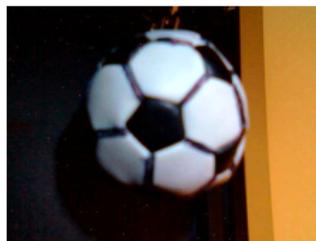
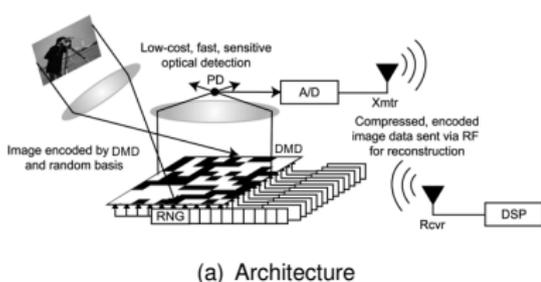


Figure: Single pixel camera



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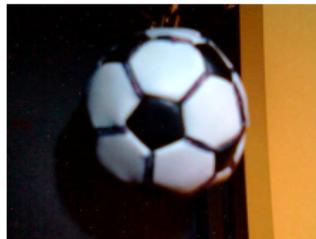
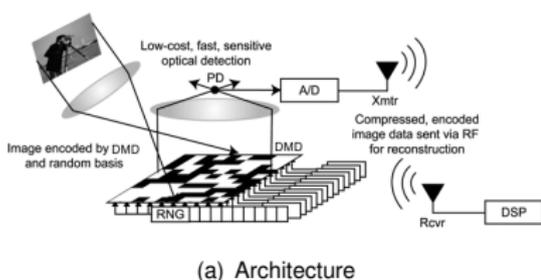


Figure: Single pixel camera



An introduction to compressive sensing

Operator description

- Linear operator (linear algebra) representation of **signal decomposition**:

$$x(t) = \sum_i \alpha_i \Psi_i(t) \quad \rightarrow \quad \mathbf{x} = \sum_i \Psi_i \alpha_i = \begin{pmatrix} | \\ \Psi_0 \\ | \end{pmatrix} \alpha_0 + \begin{pmatrix} | \\ \Psi_1 \\ | \end{pmatrix} \alpha_1 + \dots \quad \rightarrow \quad \boxed{\mathbf{x} = \Psi \alpha}$$

- Linear operator (linear algebra) representation of **measurement**:

$$y_i = \langle x, \Phi_j \rangle \quad \rightarrow \quad \mathbf{y} = \begin{pmatrix} - \Phi_0 - \\ - \Phi_1 - \\ \vdots \end{pmatrix} \mathbf{x} \quad \rightarrow \quad \boxed{\mathbf{y} = \Phi \mathbf{x}}$$

- Putting it together:

$$\boxed{\mathbf{y} = \Phi \mathbf{x} = \Phi \Psi \alpha}$$



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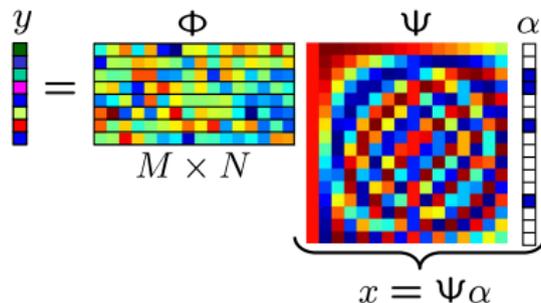
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- Putting it together:

$$\boxed{y = \Phi x = \Phi \Psi \alpha}$$



An introduction to compressive sensing

Promoting sparsity via ℓ_1 minimisation

- Ill-posed inverse problem:

$$y = \Phi x + n = \Phi \Psi \alpha + n$$

- Recall norms given by:

$$\|\alpha\|_0 = \text{no. non-zero elements} \quad \|\alpha\|_1 = \sum_i |\alpha_i| \quad \|\alpha\|_2 = \left(\sum_i |\alpha_i|^2 \right)^{1/2}$$

- Solve by imposing a regularising prior that the signal to be recovered is sparse in Ψ , *i.e.* solve the following ℓ_0 optimisation problem:

$$\alpha^* = \arg \min_{\alpha} \|\alpha\|_0 \text{ such that } \|y - \Phi \Psi \alpha\|_2 \leq \epsilon$$

where the signal is synthesising by $x^* = \Psi \alpha^*$.

- Solving this problem is **difficult** (combinatorial).
- Instead, solve the ℓ_1 optimisation problem (convex):

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An introduction to compressive sensing

Promoting sparsity via ℓ_1 minimisation

- Solutions of the ℓ_0 and ℓ_1 problems are often the same.
- Restricted isometry property (RIP):

$$(1 - \delta_K) \|\alpha\|_2^2 \leq \|\Theta\alpha\|_2^2 \leq (1 + \delta_K) \|\alpha\|_2^2,$$

for K -sparse α , where $\Theta = \Phi\Psi$.



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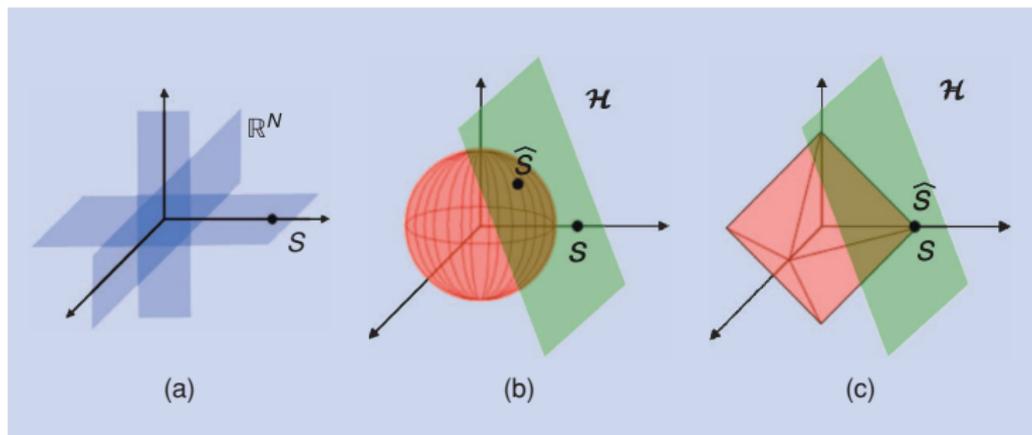


Figure: Geometry of (a) ℓ_0 (b) ℓ_2 and (c) ℓ_1 problems. [Credit: Baraniuk (2007)]



An introduction to compressive sensing

Coherence

- In the absence of noise, compressed sensing is **exact!**
- Number of measurements required to achieve exact reconstruction is given by

$$M \geq c\mu^2 K \log N,$$

where K is the sparsity and N the dimensionality.

- The coherence between the measurement and sparsity basis is given by

$$\mu = \sqrt{N} \max_{i,j} |\langle \Psi_i, \Phi_j \rangle|.$$

- Robust to noise.



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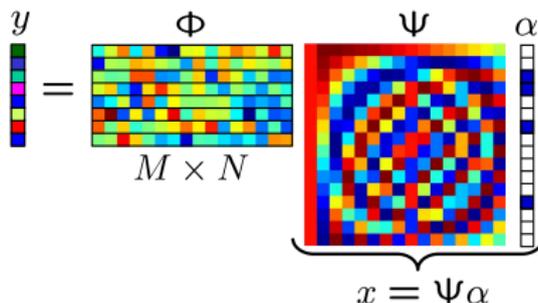
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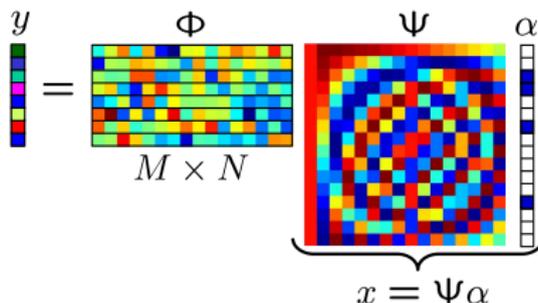
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Analysis vs synthesis

- Many new developments (e.g. analysis vs synthesis, cosparsity, structured sparsity).
- Synthesis-based framework:

$$\alpha^* = \arg \min_{\alpha} \|\alpha\|_1 \text{ such that } \|y - \Phi\Psi\alpha\|_2 \leq \epsilon.$$

where we synthesise the signal from its recovered wavelet coefficients by $x^* = \Psi\alpha^*$.

- Analysis-based framework:

$$x^* = \arg \min_x \|\Psi^T x\|_1 \text{ such that } \|y - \Phi x\|_2 \leq \epsilon,$$

where the signal x^* is recovered directly.

- Concatenating dictionaries (Rauhut *et al.* 2008) and sparsity averaging (Carrillo, McEwen & Wiaux 2013)

$$\Psi = [\Psi_1, \Psi_2, \dots, \Psi_q].$$



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Interferometric imaging with compressed sensing

- Solve the interferometric imaging problem

$$y = \Phi x + n \quad \text{with} \quad \Phi = \text{MFCA} ,$$

by applying a **prior on sparsity** of the signal in a **sparsifying dictionary** Ψ .

- Basis pursuit (BP) denoising problem

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- Total Variation (TV) denoising problem

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- Various choices for sparsifying dictionary Ψ , e.g. Dirac basis, Daubechies wavelets.



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SARA for radio interferometric imaging

Algorithm

- Sparsity averaging reweighted analysis (**SARA**) for RI imaging (Carrillo, McEwen & Wiaux 2012)
- Consider a dictionary composed of a concatenation of orthonormal bases, i.e.

$$\Psi = \frac{1}{\sqrt{q}} [\Psi_1, \Psi_2, \dots, \Psi_q],$$

thus $\Psi \in \mathbb{R}^{N \times D}$ with $D = qN$.

- We consider the following bases: Dirac (i.e. pixel basis); Haar wavelets (promotes gradient sparsity); Daubechies wavelet bases two to eight.
 \Rightarrow concatenation of 9 bases
- Promote average sparsity by solving the reweighted ℓ_1 analysis problem:

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where $W \in \mathbb{R}^{D \times D}$ is a diagonal matrix with positive weights.

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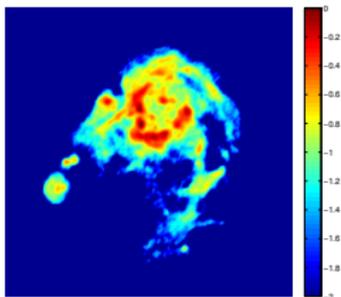
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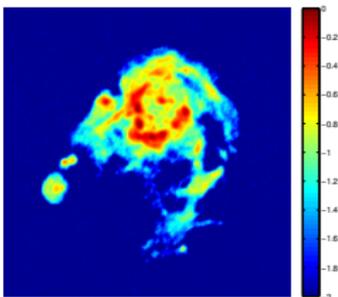


SARA for radio interferometric imaging

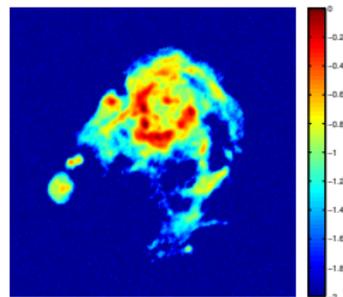
Results on simulations



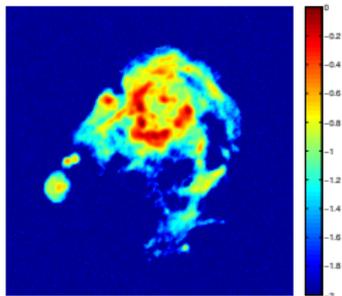
(a) Original



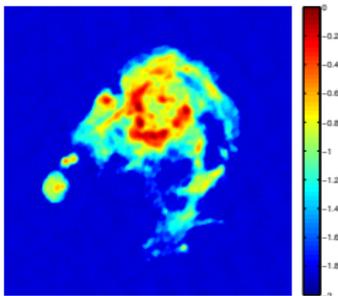
(b) BP (SNR=32.82 dB)



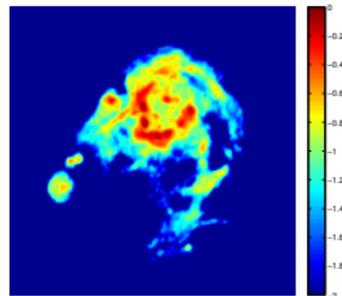
(c) IUWT (SNR=32.12 dB)



(d) BPD_{b8} (SNR=33.70 dB)



(e) TV (SNR=33.89 dB)

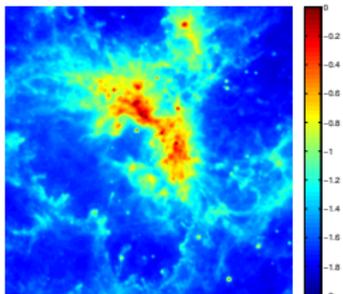


(f) SARA (SNR=38.43 dB)

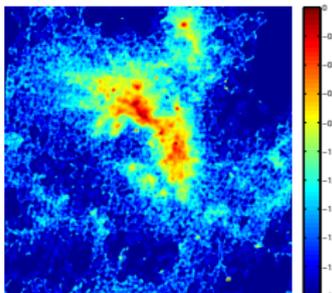


SARA for radio interferometric imaging

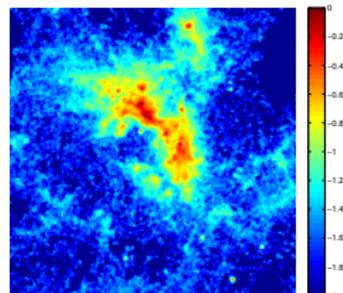
Results on simulations



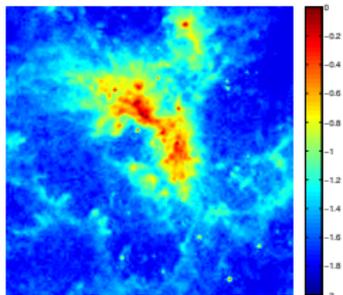
(a) Original



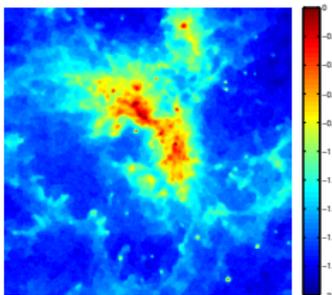
(b) BP (SNR=16.67 dB)



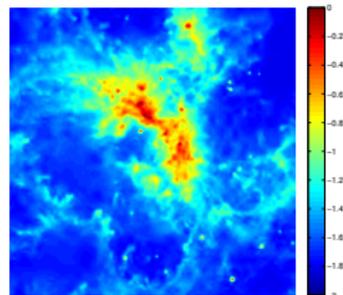
(c) IUWT (SNR=17.87 dB)



(d) BPDb8 (SNR=24.53 dB)



(e) TV (SNR=26.47 dB)

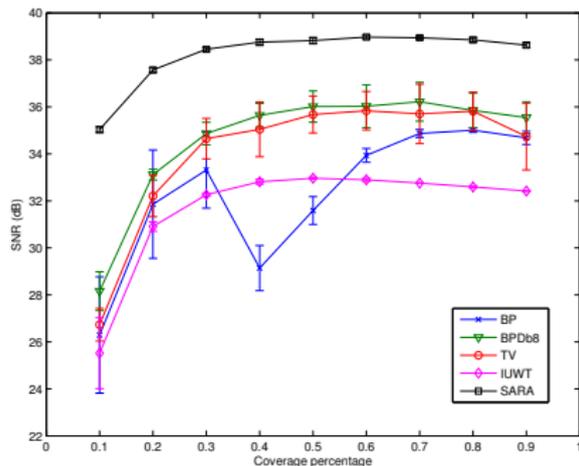


(f) SARA (SNR=29.08 dB)

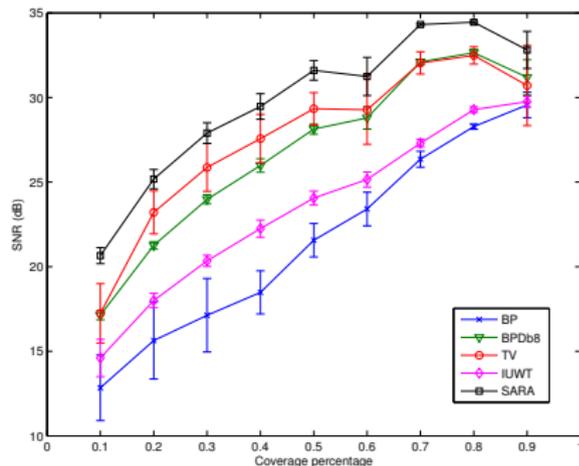


SARA for radio interferometric imaging

Results on simulations



(a) M31



(b) 30Dor

Figure: Reconstruction fidelity vs visibility coverage.



Outline

- 1 Radio Interferometry (RI)
- 2 Compressive Sensing (CS)
- 3 Radio Interferometric Imaging with Compressive Sensing (RI+CS)
- 4 Spread Spectrum**
- 5 Continuous Visibilities
- 6 Outlook



Review of the spread spectrum effect

- **Wide field** $\rightarrow w$ -modulation \rightarrow spread spectrum effect first considered by Wiaux *et al.* (2009b).
- The w -modulation operator \mathbf{C} has elements defined by

$$C(l, m) \equiv e^{i2\pi w(1 - \sqrt{1 - l^2 - m^2})} \simeq e^{i\pi w \|l\|^2} \quad \text{for } \|l\|^4 w \ll 1,$$

giving rise to to a linear chirp.

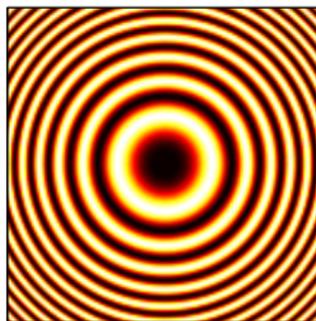


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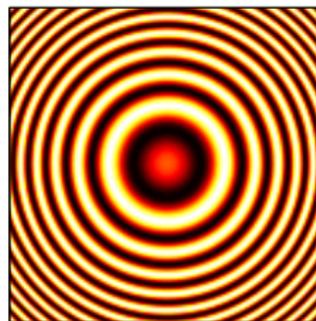
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(a) Real part



(b) Imaginary part

Figure: Chirm modulation.



Review of the spread spectrum effect

- For the (essentially) Fourier measurements of interferometric telescopes the coherence is the maximum modulus of the Fourier coefficients of atoms of the sparsifying dictionary.
- w -modulation spreads the spectrum of the atoms of the sparsifying dictionary.
- Consequently, spreading the spectrum increases the incoherence between the sensing and sparsity bases, thus improving reconstruction fidelity.
- Improved reconstruction fidelity of the spread spectrum effect demonstrated with simulations by Wiaux *et al.* (2009b).
- However, previous analysis was restricted to constant w for simplicity.
- Examined the spread spectrum effect for varying w .
- Work of Laura Wolz in collaboration with McEwen, Abdalla, Carrillo and Wiaux (see Wolz *et al.* 2013).



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Spread spectrum effect for varying w

w -projection

- Apply the w -projection algorithm (Cornwell *et al.* 2008) to shift the chirp modulation through the Fourier transform:

$$\Phi = \mathbf{MFC}\mathbf{A} \Rightarrow \Phi = \hat{\mathbf{C}}\mathbf{F}\mathbf{A}$$

- Consider different w for each (u, v) and threshold each Fourier transformed chirp (each row of $\hat{\mathbf{C}}$) to approximate $\hat{\mathbf{C}}$ accurately by a sparse matrix.
- Retain $E\%$ of the energy content of the w -modulation for each visibility measurement (typically $E = 75\%$).
- Support of w -modulation in Fourier space determined dynamically.



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Spread spectrum effect for varying w

Approximation of w -modulation kernel

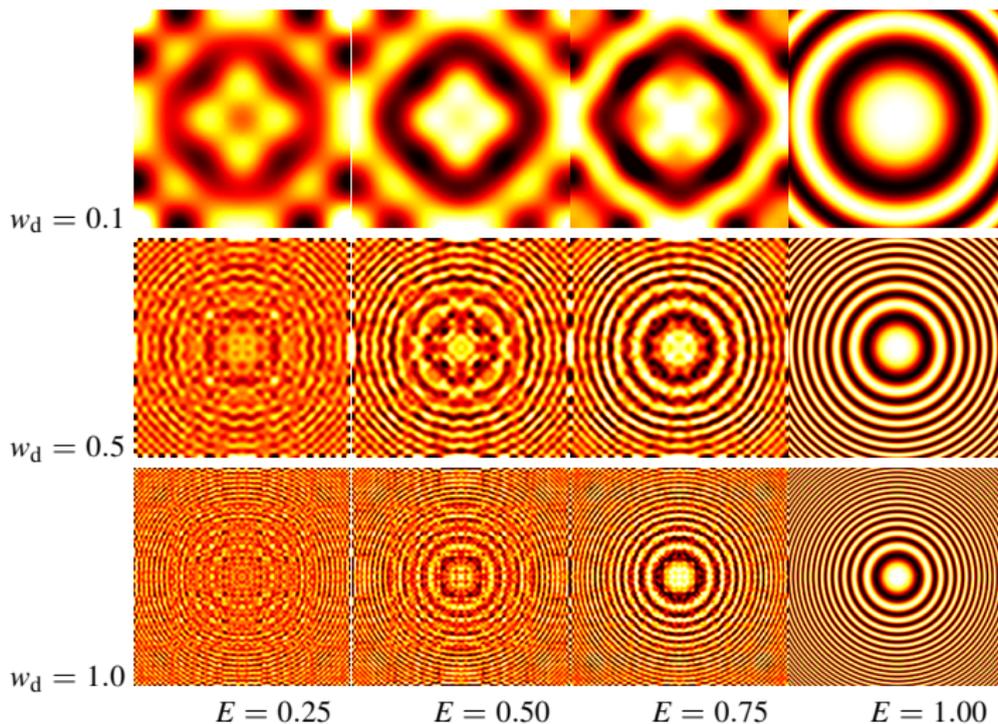


Figure: w -modulation kernel.



Spread spectrum effect for varying w

Impact of approximation of w -modulation kernel

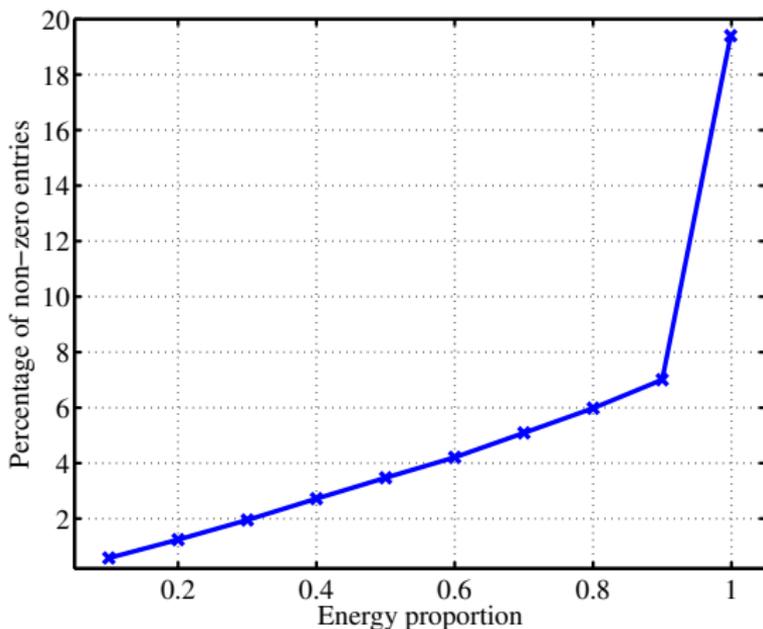


Figure: Percentage of non-zero entries as a function of preserved energy proportion.



Spread spectrum effect for varying w

Impact of approximation of w -modulation kernel

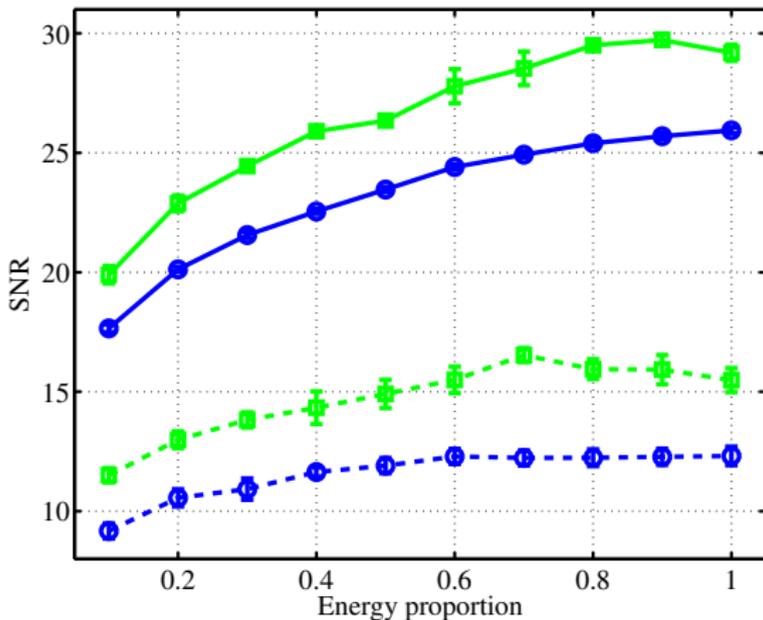


Figure: Reconstruction quality of M31 (green lines marked with squares) and 30Dor (blue lines marked with circles) as a function of preserved energy proportion for visibility coverages 10% (dashed) and 50% (solid).



Spread spectrum effect for varying w

Results on simulations

- Perform simulations to assess the effectiveness of the spread spectrum effect in the presence of **varying** w .
- Consider idealised simulations with uniformly random visibility sampling.

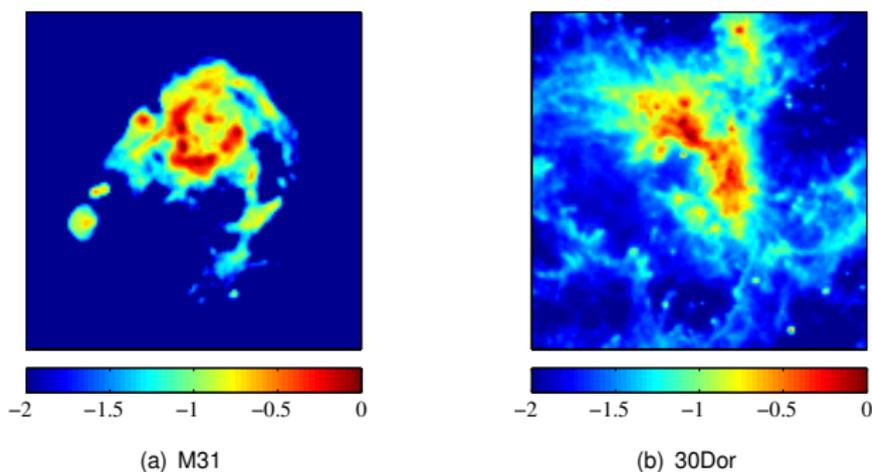
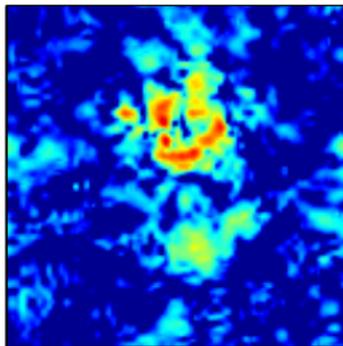


Figure: Ground truth images in logarithmic scale.



Spread spectrum effect for varying w

Results on simulations



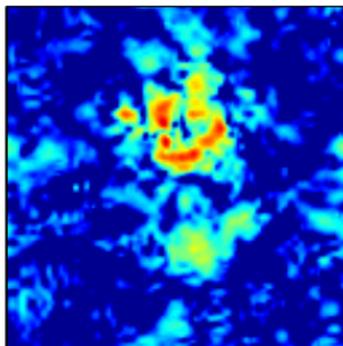
(a) $w_d = 0 \rightarrow \text{SNR} = 5\text{dB}$

Figure: Reconstructed images of M31 for 10% coverage.

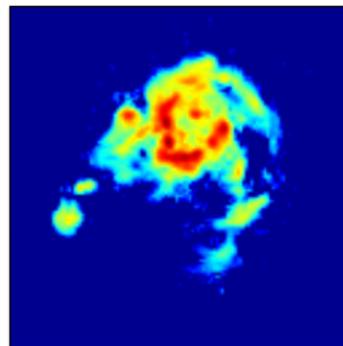


Spread spectrum effect for varying w

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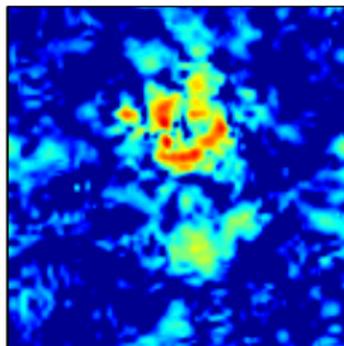
(c) $w_d = 1 \rightarrow \text{SNR} = 19\text{dB}$

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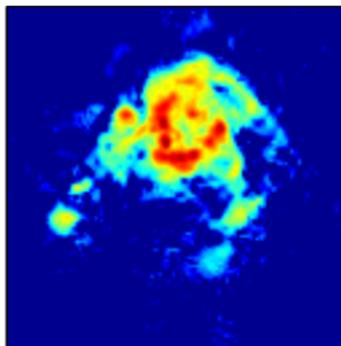


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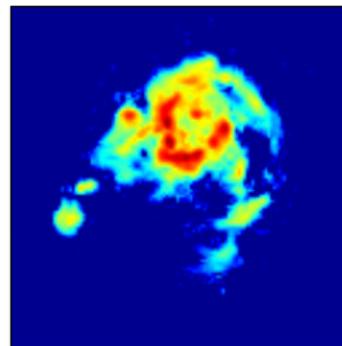
Results on simulations



(a) $w_d = 0 \rightarrow \text{SNR} = 5\text{dB}$



(b) $w_d \sim \mathcal{U}(0, 1) \rightarrow \text{SNR} = 16\text{dB}$



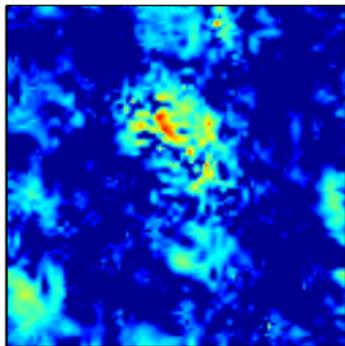
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Spread spectrum effect for varying w

Results on simulations



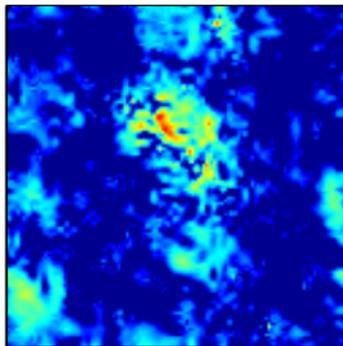
(a) $w_d = 0 \rightarrow \text{SNR} = 2\text{dB}$

Figure: Reconstructed images of 30Dor for 10% coverage.

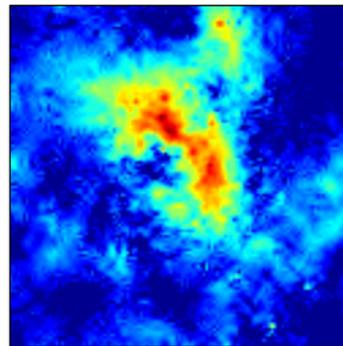


Spread spectrum effect for varying w

Results on simulations



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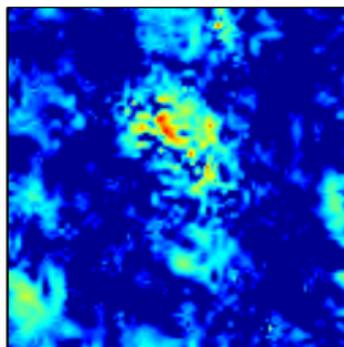
(c) $w_d = 1 \rightarrow \text{SNR} = 15\text{dB}$

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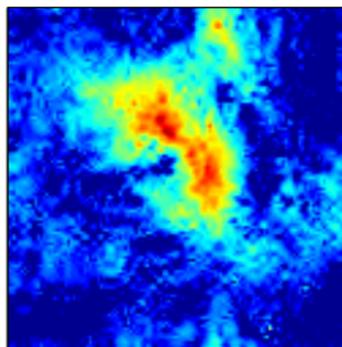


Spread spectrum effect for varying w

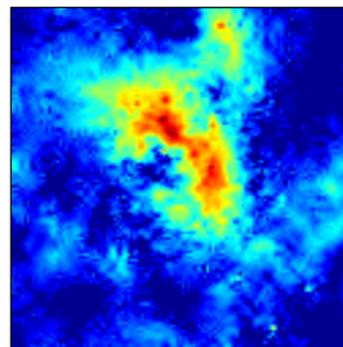
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(a) $w_d = 0 \rightarrow \text{SNR} = 2\text{dB}$



(b) $w_d \sim \mathcal{U}(0, 1) \rightarrow \text{SNR} = 12\text{dB}$



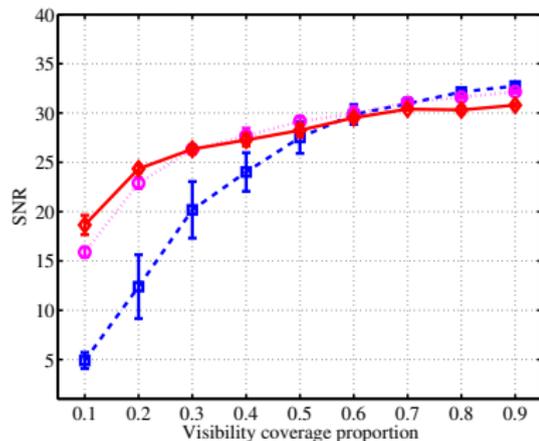
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Figure: Reconstructed images of 30Dor for 10% coverage.



Spread spectrum effect for varying w

Results on simulations



(a) Daubechies 8 (Db8) wavelets

Figure: Reconstruction fidelity for M31.

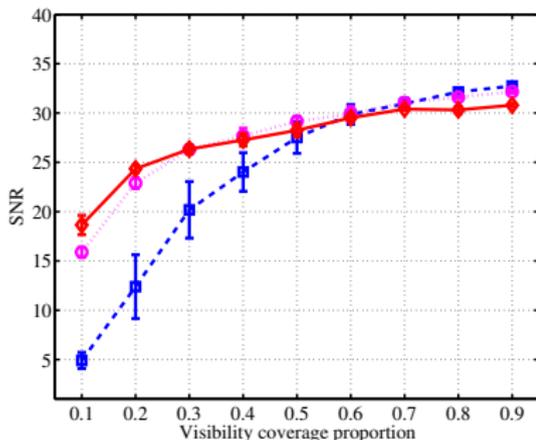
Improvement in reconstruction fidelity due to the spread spectrum effect for varying w is almost as large as the case of constant maximum w !

- As expected, for the case where coherence is already optimal, there is little improvement.



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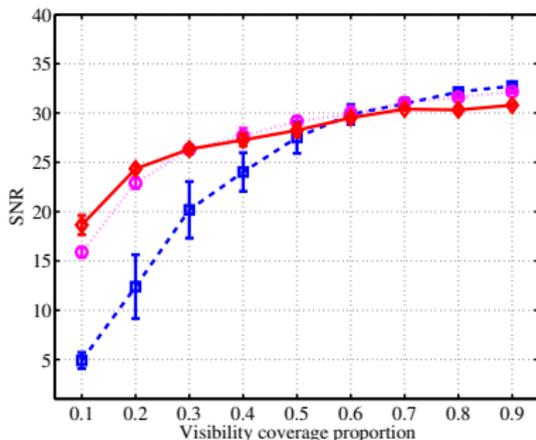
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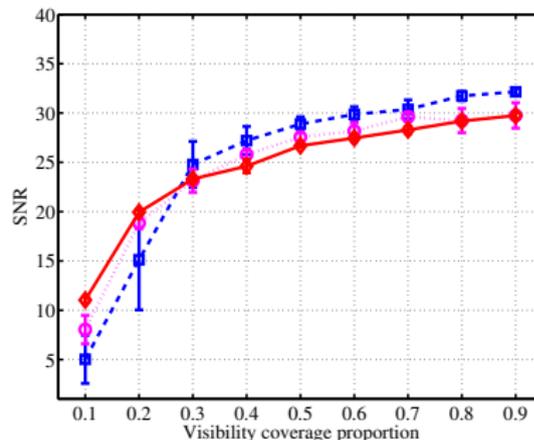


Spread spectrum effect for varying w

Results on simulations



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(b) Dirac basis

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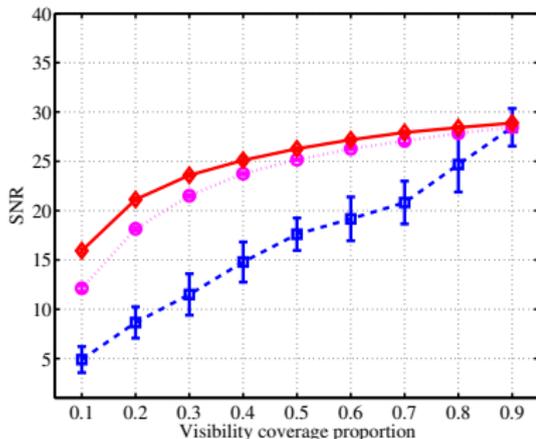
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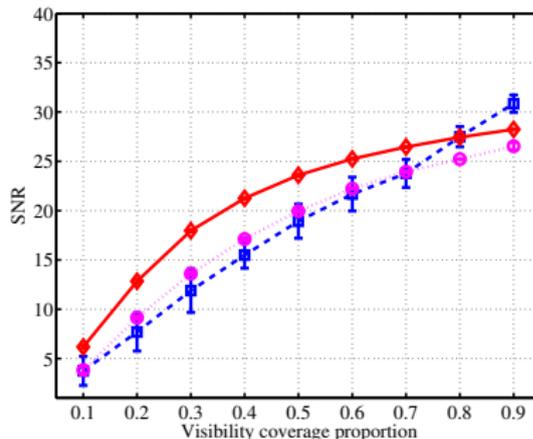


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Supporting continuous visibilities

Algorithm

- Ideally we would like to model the continuous Fourier transform operator

$$\Phi = \mathbf{F}^c .$$

- But this is impracticably slow!
- Incorporated gridding into our CS interferometric imaging framework.
- Work of Rafael Carrillo, in collaboration with Wiaux and McEwen (see Carrillo, McEwen, Wiaux 2013).
- Model with measurement operator

$$\Phi = \mathbf{GFDZ} ,$$

where we incorporate:

- convolutional gridding operator \mathbf{G} ;
- fast Fourier transform \mathbf{F} ;
- normalisation operator \mathbf{D} to undo the convolution gridding;
- zero-padding operator \mathbf{Z} to upsample the discrete visibility space.



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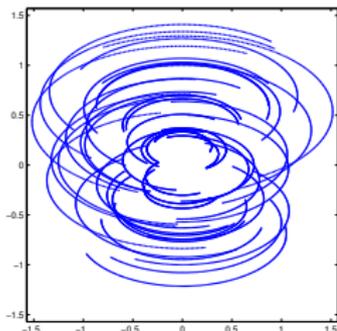
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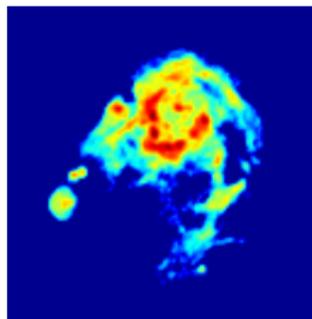


Supporting continuous visibilities

Results on simulations



(a) Coverage

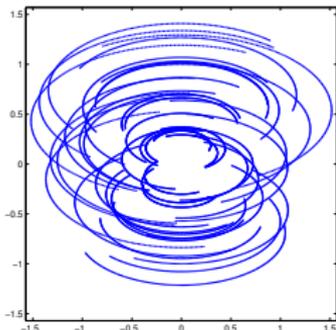


(b) M31 (ground truth)

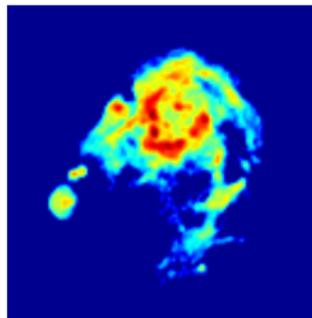


Supporting continuous visibilities

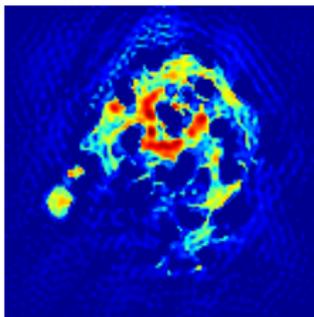
Results on simulations



(a) Coverage



(b) M31 (ground truth)

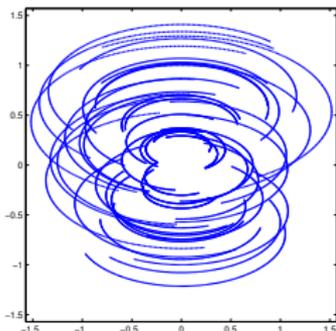


(c) Dirac basis \rightarrow SNR= 8.2dB

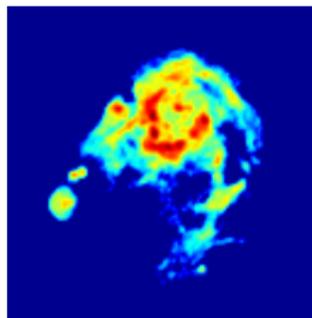


Supporting continuous visibilities

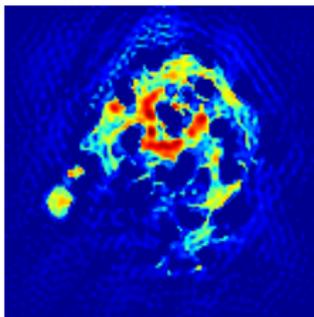
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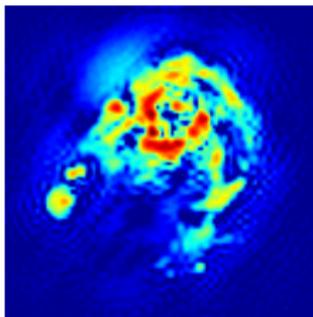
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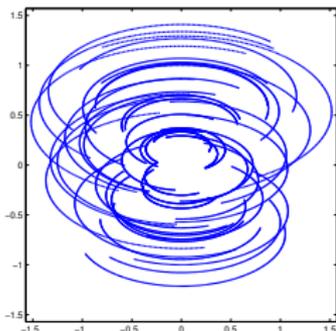


(d) Db8 wavelets \rightarrow SNR= 11.1dB

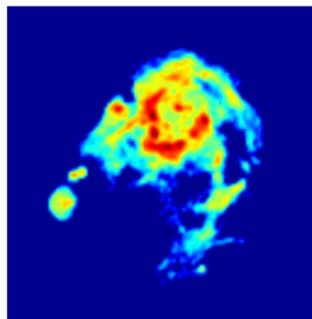


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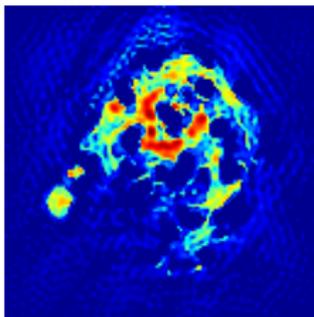
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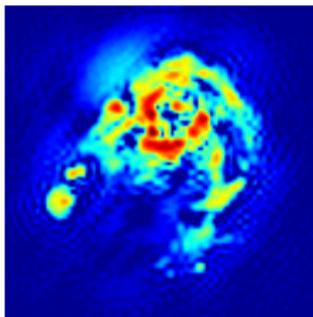
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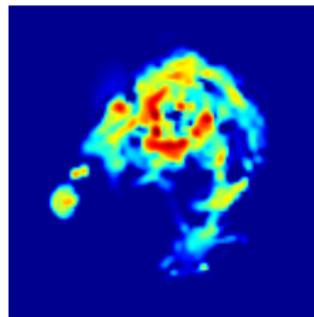
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(d) Db8 wavelets \rightarrow SNR= 11.1dB



(e) SARA \rightarrow SNR= 13.4dB



Outline

- 1 Radio Interferometry (RI)
- 2 Compressive Sensing (CS)
- 3 Radio Interferometric Imaging with Compressive Sensing (RI+CS)
- 4 Spread Spectrum
- 5 Continuous Visibilities
- 6 Outlook



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- **Effectiveness of compressive sensing** for radio interferometric imaging demonstrated (Wiaux *et al.* 2009a, Wiaux *et al.* 2009b, Wiaux *et al.* 2009c, McEwen & Wiaux 2011, Carrillo *et al.* 2012).
- Important to take these methods to the **realistic setting** so that their advantages can be realised on observations made by real radio interferometric telescopes.
- Taken first steps toward more **realistic setting**.
- **Wide fields**: studied the spread spectrum effect for **varying w** (Wolz *et al.* 2013).
- **Continuous visibilities**: incorporated **gridding** operator (Carrillo *et al.* 2013).



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- Includes state-of-the-art convex optimisation algorithms that support parallelisation.
- Plan to perform more extensive comparisons with traditional techniques, such as CLEAN, MS-CLEAN and MEM.

Apply to observations made by real interferometric telescopes.

PURIFY code

<http://basp-group.github.io/purify/>



Next-generation radio interferometric imaging

Carrillo, McEwen, Wiaux

PURIFY is an open-source code that provides functionality to perform radio interferometric imaging, leveraging recent developments in the field of compressive sensing and convex optimisation.



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